

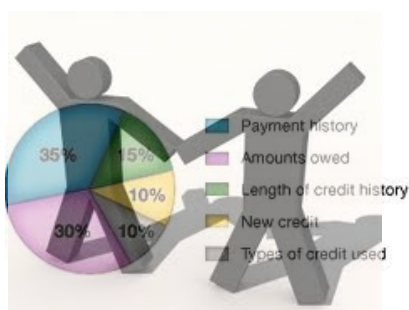
## Why do we teach/learn math?



"to get to seven-eleven and back successfully"

- $+$   $-$   $\times$   $\div$
- decimals
- money

## Why do we teach/learn math?



"so we can figure out our budget, like car payments, mortgages, take-home pay"

- decimals, percent
- interest
- maybe formula substitution

"hey Mr F.....they do that for you!"

## Why do we teach/learn math?



"ok.....what about the f word?"

f ..... (a c t) (o r) (i n g)

"Keep it real man"

## Why do we teach/learn math?

We divide it by  $m(x) = x^2 + 2x + 1$  and take the remainder:

$$\begin{array}{r}
 \text{Dividend: } x^3 + 3x^2 + 4x + 1 \\
 \text{Divisor: } x^2 + 2x + 1 \\
 \hline
 \text{Quotient: } x + 1 \\
 \text{Remainder: } 2x + 1
 \end{array}$$

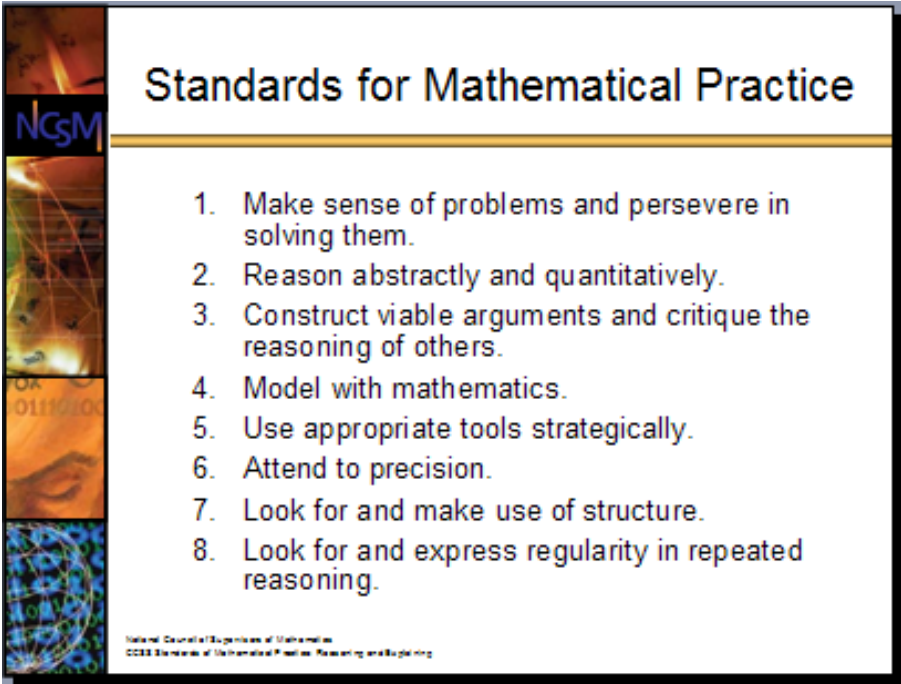
Note how the b's are shifted left by 1 spot.

This is just  $b_1$  multiplied by a small polynomial.

"truth is.....calculus is the place where math and the real world merge"

- related rates
- min/max
- applications of derivatives and integrals
- the sciences and engineering

SO..... Why do we teach/learn math?

A graphic titled "Standards for Mathematical Practice" with a vertical strip of images on the left. The images include mathematical symbols like pi and infinity, the acronym "NGSM", a hand holding a pen, and a globe. The main content is a numbered list of eight practices.

**Standards for Mathematical Practice**

1. Make sense of problems and persevere in solving them.
2. Reason abstractly and quantitatively.
3. Construct viable arguments and critique the reasoning of others.
4. Model with mathematics.
5. Use appropriate tools strategically.
6. Attend to precision.
7. Look for and make use of structure.
8. Look for and express regularity in repeated reasoning.

National Council of Teachers of Mathematics  
CCSS Standards of Mathematical Practice: Reasoning and Exploring

What if every student K-12 becomes proficient at this set?

the eight practice standards for  
mathematics taken from CCSS

## We teach/learn math to Practice the Practices (SMP CCSS)

The Standards for Mathematical Practice describe varieties of expertise that mathematics educators at all levels should seek to develop in our students.....

CCSS p6

So factoring was "real life" !

$$2x^2-12x+16$$



- what do I do first?
- If I do this...I could be wrong
- but I've been practicing .....
- I know the procedures
- if I'm wrong I'll know because....
- I've checked it and it's good



(a short example)



they're in there.....

6/22/11 NYSUT's Teacher Practice Rubrics

**Element L2: Teachers demonstrate current, research-based knowledge of learning and language acquisition theories and processes.**  
**NYSED Indicators:** Design lesson plans and adjust instruction to include a variety of strategies that support the learning needs of each student. Design lesson plans and adjust instruction to include a variety of strategies that support the language acquisition needs of each student. Teachers explain their instructional decisions citing current research.

	Indicators	Ineffective	Developing	Effective	Highly Effective
A	Uses strategies to support	Teacher designs lessons	Teacher designs lessons to	Teacher designs lessons to	Teacher designs lessons

Marzano's Rubric

8. Previewing New Content
The teacher engages students in activities that help them link what they already know to the new content about to be addressed and facilitates these linkages.
<p><b>Teacher Evidence</b></p> <ul style="list-style-type: none"> <li><input type="checkbox"/> Teacher uses preview question before reading</li> <li><input type="checkbox"/> Teacher uses K-W-L strategy or variation of it</li> <li><input type="checkbox"/> Teacher asks or reminds students what they already know about the topic</li> <li><input type="checkbox"/> Teacher provides an advanced organizer                             <ul style="list-style-type: none"> <li>• Outline</li> <li>• Graphic organizer</li> </ul> </li> <li><input type="checkbox"/> Teacher has students brainstorm</li> <li><input type="checkbox"/> Teacher uses anticipation guide</li> <li><input type="checkbox"/> Teacher uses motivational hook/launching activity                             <ul style="list-style-type: none"> <li>• Anecdotes</li> <li>• Short selection from video</li> </ul> </li> <li><input type="checkbox"/> Teacher uses word splash activity to connect vocabulary to upcoming content</li> </ul>
<p><b>Student Evidence</b></p> <ul style="list-style-type: none"> <li><input type="checkbox"/> When asked, students can explain linkages with prior knowledge</li> <li><input type="checkbox"/> When asked, students make predictions about upcoming content</li> <li><input type="checkbox"/> When asked, students can provide a purpose for what they are about to learn</li> <li><input type="checkbox"/> Students actively engage in previewing activities</li> </ul>

Danielson's Rubric

Component	3c: Engaging Students in Learning
	<p>Student engagement in learning is the centerpiece of the framework for teaching; all other components contribute to it. When students are engaged in learning, they are not merely "busy," nor are they only "on task." Rather, they are intellectually active in learning important and challenging content. The critical distinction between a classroom in which students are compliant and busy, and one in which they are engaged, is that in the latter students are developing their understanding through what they do. That is, they are engaged in discussion, debate, answering "what if?" questions, discovering patterns, and the like. They may be selecting their work from a range of (teacher arranged) choices, and making important contributions to the intellectual life of the class. Such activities don't typically consume an entire lesson, but they are essential components of engagement.</p> <p>A lesson in which students are engaged usually has a discernible structure: a beginning, a middle, and an end, with scaffolding provided by the teacher or by the activities themselves. Student tasks are organized to provide cognitive challenge, and then students are encouraged to reflect on what they have done and what they have learned. That is, there is closure to the lesson, in which students derive the important learning from their own actions. A critical question for an observer in determining the degree of student engagement is "What are the students being asked to do?" If the answer to that question is that they are filling in blanks on a worksheet, or performing a rote procedure, they are unlikely to be cognitively engaged.</p>

## Implementation of the SMP

- math classes that are not boring
- stop "covering"
- rich problems
- addressing formative assessments
- utilizing data

If I'm doing those things.....bring on APPR

## Where are these Rich Problems

### from Diane Briars NCSM

**McDonald's Claim**

A recent Wikipedia article reports that 8% of all Americans eat at McDonald's every day. Current data indicates approximately 310 million Americans and 12,800 McDonald's restaurants in the United States.

Do you believe the Wikipedia report to be true? Create a mathematical argument to justify your position.

### from engageny.org

Make true equations. Write one number in every space. Draw a picture if it helps.

- 1) 1 hundred + 4 tens = \_\_\_\_\_
- 2) 4 tens + 1 hundred = \_\_\_\_\_
- 3) 14 tens = 10 tens + \_\_\_\_\_ tens  
= \_\_\_\_\_ hundred + 4 tens  
= \_\_\_\_\_
- 4) 7 ones + 5 hundreds = \_\_\_\_\_
- 5) 8 hundreds = \_\_\_\_\_
- 6) 106 = 1 hundred + \_\_\_\_\_ tens + \_\_\_\_\_ ones
- 7) 106 = \_\_\_\_\_ tens + \_\_\_\_\_ ones
- 8) 106 = \_\_\_\_\_ ones
- 9)  $90 + 300 + 4 =$  \_\_\_\_\_

Are these comparisons true or false?

- 10)  $2 \text{ hundreds} + 3 \text{ ones} > 5 \text{ tens} + 9 \text{ ones}$  \_\_\_\_\_
- 11)  $9 \text{ tens} + 2 \text{ hundreds} + 4 \text{ ones} < 924$  \_\_\_\_\_
- 12)  $456 < 5 \text{ hundreds}$  \_\_\_\_\_

### from NCTM

Homework #16- Falling Bridges!

Thorough Ted, a construction engineer, correctly computed that the maximum safe load of a bridge being planned would be  $1000(99-70\sqrt{2})$  tons. Speedy Sam, a construction contractor, then approximated  $\sqrt{2}$  as 1.4.

The bridge was built and a sign was posted, based on Speedy Sam's calculations, saying how much weight the bridge could safely hold. On the day it opened to traffic, the bridge collapsed under a load less than a tenth of the posted weight.

### from insidemathematics.org

#### Winning Lines

This problem gives you the chance to:  
• work with a 'magic square' type number game

Gina and Sam are playing a card game. They place number cards on a large game board. A target number is written inside a circle at the top of each board.

14		
7	6	1
5	3	9
2	8	4

To win a point they need to make a line of three numbers whose sum is the target number. The three numbers can be written in a column, a row or a diagonal.

In any game the same number cannot be used more than twice. No zeros are allowed.

1. Gina and Sam have completed the game shown above. The target number is 14. Draw lines through the five winning lines.

12		
4		
3		
5		

2. Here is a game board that has already been started. One point has been won because  $4 + 3 + 5 = 12$ . Write numbers on the empty cards to win at least three more points. Draw lines through your winning lines.

9		

3. Here is a new game board. Fill in the numbers to win at least four points. Draw in the winning lines. Explain why the number 8 cannot be used in any winning line.

Grade 4—2008  
Copyright ©2008 by Mathematics Assessment Resource Service  
All rights reserved.

7  
35

### from nys 2005 sample tasks

#### Sample of Generating and Testing a Hypotheses

**G.PS.5** Choose an effective approach to solve a problem from a variety of strategies (numeric, graphic, algebraic)

**G.PS.5a**

Students in one mathematics class noticed that a local movie theater sold popcorn in different shapes of containers, for different prices. They wondered which of the choices was the best buy. Analyze the three popcorn containers below. Which is the best buy? Explain.

